## Bellwork <br> 01/23/2012

Find the value of the variable.

1. If $x=9$ and $z=11$, find $m \angle X$ to the nearest tenth of a degree.

$$
\begin{aligned}
& \sin x=\frac{9}{11} \\
& m \angle x=\sin ^{-1}\left(\frac{9}{11}\right)
\end{aligned}
$$


$m \angle X=54.9^{\circ}$
2. If $y=5$ and $z=12$, find $m<X$
to the nearest tenth of a degree.

$$
\begin{aligned}
& \cos x=\frac{5}{12} \\
& m \angle x=\cos ^{-1}\left(\frac{5}{12}\right) \\
& m \angle x=65.4^{\circ}
\end{aligned}
$$

## Geometry

### 8.1 Find Angle Measures in Polygons Standard(s): 2, 4

## Vocabulary:

Consecutive Vertices: Two vertices that are endpoints of the same side.

Diagonal: A segment that joins two nonconsecutive vertices.

## THEOREMS

TheOrem 8.1 Polygon Interior Angles Theorem
The sum of the measures of the interior angles of a convex $n$-gon is $(n-2) \cdot 180^{\circ}$.
$m \angle 1+m \angle 2+\cdots+m \angle n=(n-2) \cdot 180^{\circ}$
Proof: Ex. 33, p. 512 (for pentagons)


COROLLARY TO Theorem 8.1 Interior Angles of a Quadrilateral
The sum of the measures of the interior angles of a quadrilateral is $360^{\circ}$.
Proof: Ex. 34, p. 512

## THEOREM

For Your Notebook
THEOREM 8.2 Polygon Exterior Angles Theorem
The sum of the measures of the exterior angles of a convex polygon, one angle at each vertex, is $360^{\circ}$.
$m \angle 1+m \angle 2+\cdots+m \angle n=360^{\circ}$
Proof: Ex. 35, p. 512


Sum of Interior $\angle \mathrm{s}$ : $\quad 180(\mathrm{n}-2)$
Interior _of Regular: $\frac{180(n-2)}{n}$
Sum of Interior «'s of Quad: 360
Sum of Exterior $\left\llcorner\right.$ 's: $360^{\circ}$
Exterior < of Regular:

Find the Sum of Angles in Polygons
Find the sum of the measures of the interior angles of the convex polygon.
$180(n-2)$
11-gon
$n=11$
$180(11-2)$
$180(9)$
$1620^{\circ}$
15-gon


Find the \# of Sides
The sum of the measures of the interior angles of a convex polygon is given. Classify the polygon by the number of sides.

$$
\begin{aligned}
& 1800^{\circ} \\
& \begin{array}{c}
\frac{18 \phi(n-2)}{180}=\frac{180 \phi}{18 \phi} \\
n-2=10 \\
+2+2
\end{array} \\
& 2520^{\circ} n=12
\end{aligned}
$$

$$
\begin{gathered}
3960^{\circ} \\
\frac{180}{180}(n-2)=\frac{3960}{180} \\
n-2=22 \\
+2+2 \\
n=24
\end{gathered}
$$

Find a Missing Value
Find the value of $x$.

$$
\begin{gathered}
180(n-2) \\
180(7-2) \\
180(5) \\
900
\end{gathered}
$$



$$
16 x+34 x+24 x+102+124+
$$

$$
16
$$

$$
74 x+530=900
$$

$74 x=370$

$$
\begin{gathered}
x+2 x+77+45+40=36 \\
3 x+162=360 \\
3 x=198 \\
x=66
\end{gathered}
$$

Regular Polygons
Find the measure of an interior and exterior angle of the indicated regular polygon.

Regular Pentagon

$$
n=5
$$

工: $\frac{180(n-2)}{n}$
$E: \frac{360}{5}$
I: $\frac{180(3)}{5}$
$E=72^{\circ}$

$$
I=108^{\circ}
$$

Regular 90-gon

$$
\begin{aligned}
& \frac{180(90-2)}{90} \\
& \frac{180(88)}{90}=\left(76^{\circ}\right)
\end{aligned}
$$

$$
\frac{360}{90}
$$



## Homework Assignment

## Worksheet 8.1B

