

Bellwork

12/05/2011

1. Simplify $\sqrt{48}$ in simplest radical form.

$$\frac{\sqrt{16} \cdot \sqrt{3}}{4\sqrt{3}}$$

Example: $\sqrt{8} = 2\sqrt{2}$

$$\frac{\sqrt{8}}{\sqrt{4} \cdot \sqrt{2}} = 2\sqrt{2}$$

2. Factor $3x^2 + 2x - 1$.

$$(3x - 1)(x + 1)$$

$$-x + 3x = 2x \checkmark$$

Geometry

6.1 Ratios, Proportions, and the Geometric Mean

Standard(s): 4,9

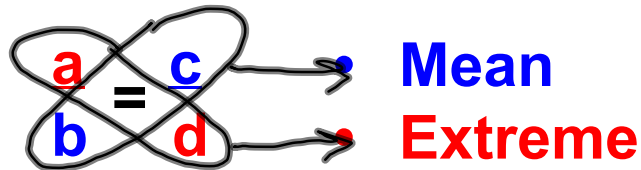
Vocabulary:

1. Ratio of a to b : If a and b are two numbers or quantities and $b \neq 0$, then the ratio is $\frac{a}{b}$.

$$a:b \quad a \text{ to } b \quad \frac{a}{b}$$

2. Proportion: An equation that states that two ratios are equal.

3. Extremes:



4. Means:

5. Geometric Mean: The square root of the product of the two numbers.

KEY CONCEPT

For Your Notebook

Geometric Mean

The geometric mean of two positive numbers a and b is the positive number x that satisfies $\frac{a}{x} = \frac{x}{b}$. So, $x^2 = ab$ and $x = \sqrt{ab}$.

Geometric Mean: Multiply the numbers and take the square root.

KEY CONCEPT

For Your Notebook

A Property of Proportions

1. **Cross Products Property** In a proportion, the product of the extremes equals the product of the means.

If $\frac{a}{b} = \frac{c}{d}$ where $b \neq 0$ and $d \neq 0$, then $ad = bc$.

$$\frac{2}{3} = \frac{4}{6} \quad \begin{array}{l} \curvearrowright 3 \cdot 4 = 12 \\ \curvearrowright 2 \cdot 6 = 12 \end{array}$$

Solve Proportions: Multiply using cross products!

Simplify Ratios

Simplify the ratio.

NOTE: Find the GCF!

A. 12km:3km

$$\frac{12 \text{ km}}{3 \text{ km}}$$

$$4 \text{ km} : 1 \text{ km}$$

B. $\frac{10 \text{ in.}}{2 \text{ ft.}}$

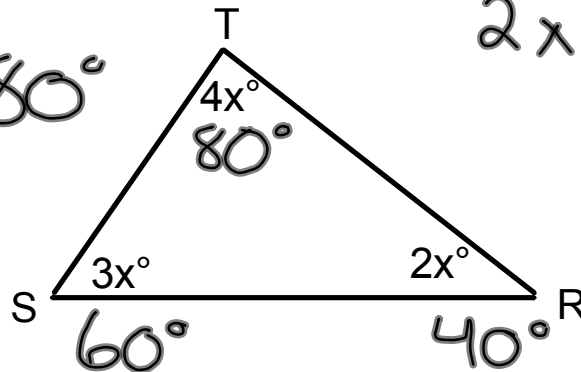
$$\frac{10 \text{ in}}{24 \text{ in}}$$

$$5 \text{ in} : 12 \text{ in}$$

Use Extended Ratios

The measure of the angles of $\triangle RST$ are in the extended ratio 2:3:4.
Find the measures of the angles.

$40^\circ, 60^\circ, 80^\circ$



$$\begin{aligned}2x + 3x + 4x &= 180 \\9x &= 180 \\x &= 20\end{aligned}$$

Attach a variable to the ratios!

Solve Proportions

Solve the proportion.

A. $\frac{2}{x+3} = \frac{5}{4x}$

$$8x = 5x + 15$$

$$3x = 15$$

$$x = 5$$

B. $\frac{6}{x+4} = \frac{x-4}{x}$

$$(x+4)(x-4) = 6x$$

$$x^2 - 4x + 4x - 16 = 6x$$

$$x^2 - 16 = 6x$$

$$-6x$$

$$x^2 - 6x - 16 = 0$$

$$(x+2)(x-8) = 0$$

$$x+2=0 \quad x-8=0$$

$$x = -2, 8$$

Use a Ratio to Find a Dimension and Variables

The area of the rectangle is 108 ft^2 , and the ratio of the length to the width is 4:3. Find the length and width of fence needed to enclose the garden.

$$l : w$$

$$4 : 3$$

$$A = 108 \text{ ft}^2$$

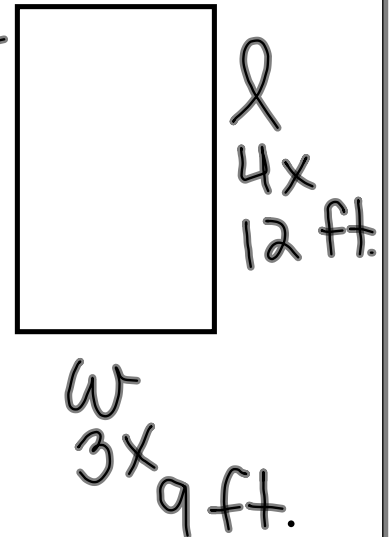
$$A = l \cdot w$$

$$108 = 4x \cdot 3x$$

$$12x^2 = 108$$

$$\sqrt{x^2} = \sqrt{9}$$

$$x = 3$$



The ratio of two side lengths for the triangle is given. Solve for the variable.

$$\frac{AB}{AC} = \frac{15}{8}$$

$AB : AC$ is $15 : 8$

$$\frac{60}{3d+2} = \frac{15}{8}$$

$$45d + 30 = 480$$

$$45d = 450$$

$$d = 10$$

Find a Geometric Mean

Find the geometric mean of the two numbers. Write the answer in simplest radical form (no decimals).

NOTE: Multiply the numbers, then take the square root!

A. 18 and 54

$$\sqrt{972}$$

$$\sqrt{324} \cdot \sqrt{3}$$

$$18\sqrt{3}$$

B. 16 and 18

$$\sqrt{288}$$

$$\sqrt{144} \cdot \sqrt{2}$$

$$12\sqrt{2}$$

Homework Assignment

Worksheet 6.1C

