

## Bellwork

### 11/16/2011

For problems 1-3, use the diagram below.  $G$  is the centroid of  $\triangle ABC$ .

1. If  $BG=9$ , find  $BF$ .

$$\frac{3}{2} \cdot 9 = \frac{2}{3} BF$$

$$BF = \frac{27}{2}$$

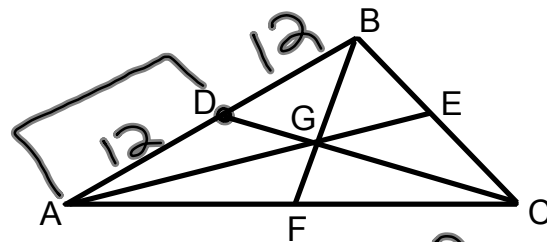
2. If  $BD=12$ , find  $AD$ .

$$AD = 12$$

3. If  $CD=27$ , find  $GC$ .

$$CG = \frac{2}{3}(27)$$

$$CG = 18$$



$$BG = \frac{2}{3} BF$$

$$CG = \frac{2}{3} CD$$

$$AG = \frac{2}{3} AE$$

## Geometry

### 5.5 Use Inequalities in a Triangle

Standard(s): 3,9

### Vocabulary:

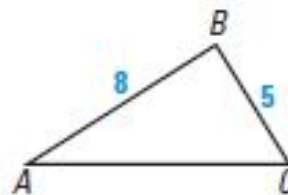
#### THEOREMS

#### For Your Notebook

##### THEOREM 5.10

If one side of a triangle is longer than another side, then the angle opposite the longer side is larger than the angle opposite the shorter side.

*Proof:* p. 329

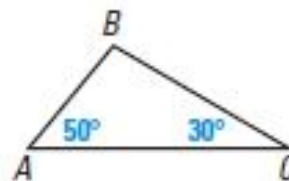


$AB > BC$ , so  $m\angle C > m\angle A$ .

##### THEOREM 5.11

If one angle of a triangle is larger than another angle, then the side opposite the larger angle is longer than the side opposite the smaller angle.

*Proof:* Ex. 24, p. 340



$m\angle A > m\angle C$ , so  $BC > AB$ .

#### THEOREM

#### For Your Notebook

##### THEOREM 5.12 Triangle Inequality Theorem

The sum of the lengths of any two sides of a triangle is greater than the length of the third side.

$$AB + BC > AC$$

$$AC + BC > AB$$

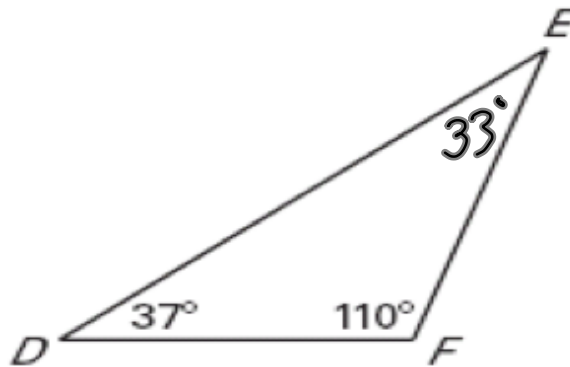
$$AB + AC > BC$$



## Relate Side Length and Angle Measure

List the sides and angles in order from least to greatest.

$\sphericalangle E, \sphericalangle D, \sphericalangle F$   
 $\overline{DF}, \overline{FE}, \overline{DE}$



## Applying the $\triangle$ Inequality Thm.

Is it possible to construct a triangle with the given side lengths? If not, explain why not.

11, 16, 32



$$11 + 16 > 32 \quad \times$$

27

No!

6, 10, 15



$$6 + 10 > 15 \quad \checkmark$$

16

$$6 + 15 > 10 \quad \checkmark$$

21

$$10 + 15 > 6 \quad \checkmark$$

25

Yes!

## Find Possible Side Lengths

Describe the possible lengths of the third side of the triangle given the lengths of the other two sides.

**12 cm, 17 cm, x cm**

$$12 + 17 > x$$

$$29 > x$$

$$x < 29 \text{ cm}$$

$$x + 12 > 17$$

$$x > 5 \text{ cm}$$

$$5 < x < 29$$

**3 yd, 5 ft**

9 ft, 5 ft, x ft

$$9 + 5 > x$$

$$14 > x$$

$$x < 14$$



When missing a side:

1. Assume it's the largest side  
small # + big # > x
2. Assume it's the smallest side  
x + small # > big #

$$x + 5 > 9$$

$$x > 4$$

$$4 < x < 14$$

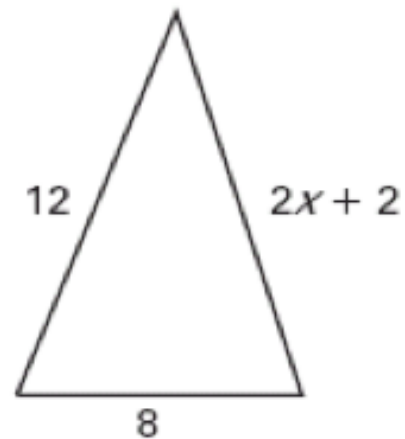
## Using $\triangle$ Inequality Algebraically

Describe the possible values of  $x$ .

$$8, 12, 2x + 2$$



$$\begin{aligned}
 1. \quad & 8 + 12 > 2x + 2 \\
 & 20 > 2x + 2 \\
 & \frac{18}{2} > \frac{2x}{2} \\
 & 9 > x \\
 & x < 9
 \end{aligned}$$



$$\begin{aligned}
 2. \quad & 2x + 2 + 8 > 12 \\
 & 2x + 10 > 12 \\
 & \frac{2x}{2} > \frac{2}{2} \\
 & x > 1
 \end{aligned}$$

$$1 < x < 9$$

# Homework Assignment

## Worksheet 5.5B

