

Pop Quiz.
Get out a scrap sheet of paper.

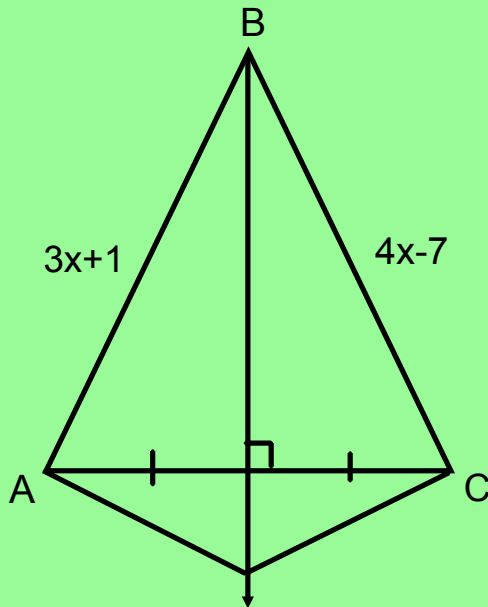
- 1. What does the midsegment theorem say we know about it's relationship with the third side?**
- 2. What does it mean for lines to be concurrent?**
- 3. What is a circumcenter?**

Bellwork

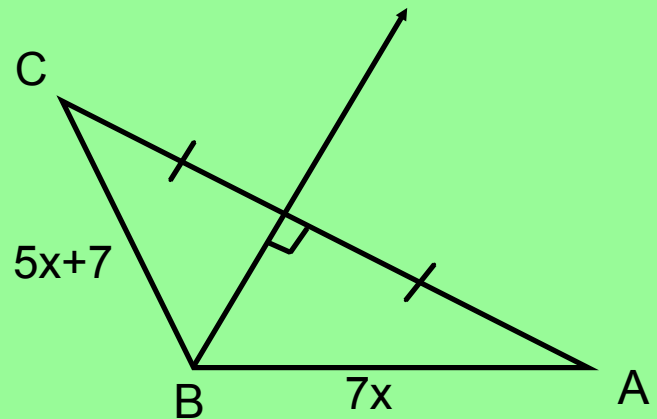
11/09/2011

In problems 1 and 2, find AB.

1.



2.



Geometry

5.3 Use Angle Bisectors of Triangles

Standard(s): 2,3

Vocabulary:

1. Incenter: The point of concurrency of the three angle bisectors of a triangle.

THEOREMS

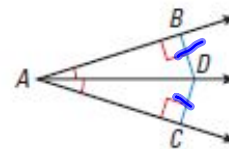
For Your Notebook

THEOREM 5.5 Angle Bisector Theorem

If a point is on the bisector of an angle, then it is equidistant from the two sides of the angle.

If \overline{AD} bisects $\angle BAC$ and $\overline{DB} \perp \overline{AB}$ and $\overline{DC} \perp \overline{AC}$, then $DB = DC$.

Proof: Ex. 34, p. 315

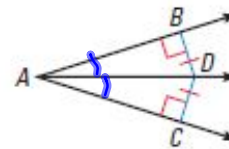


THEOREM 5.6 Converse of the Angle Bisector Theorem

If a point is in the interior of an angle and is equidistant from the sides of the angle, then it lies on the bisector of the angle.

If $\overline{DB} \perp \overline{AB}$ and $\overline{DC} \perp \overline{AC}$ and $DB = DC$, then \overline{AD} bisects $\angle BAC$.

Proof: Ex. 35, p. 315



THEOREM

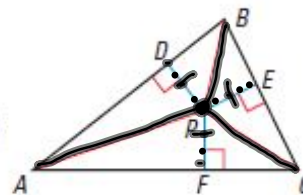
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THEOREM 5.7 Concurrency of Angle Bisectors of a Triangle

The angle bisectors of a triangle intersect at a point that is equidistant from the sides of the triangle.

If \overline{AP} , \overline{BP} , and \overline{CP} are angle bisectors of $\triangle ABC$, then $PD = PE = PF$.

Proof: Ex. 36, p. 316



Incenter

Has to ...

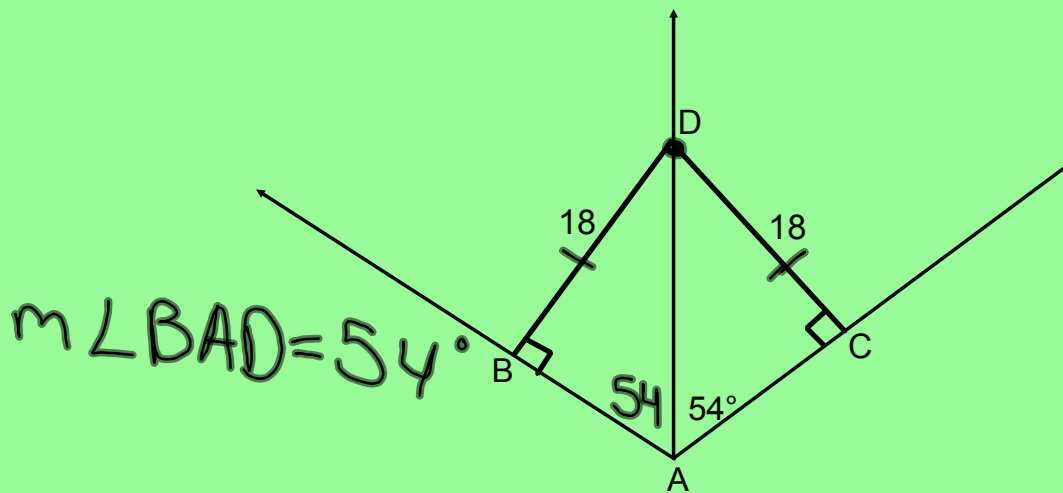
1. Be a point of intersection of the 3 \angle bisectors

Is...

1. Equidistant from the sides (\perp)

Use the Angle Bisector Theorems

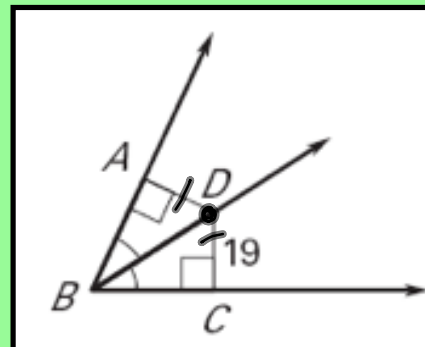
Find the measure of $\angle BAD$.



Use the information in the diagram to find the measure.

Find AD.

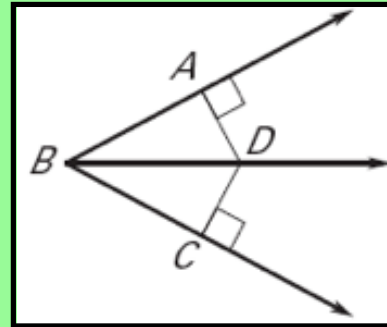
$$AD = 19$$



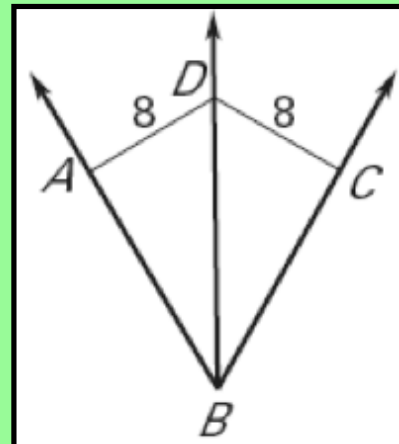
~~Solve a Real-World Problem~~

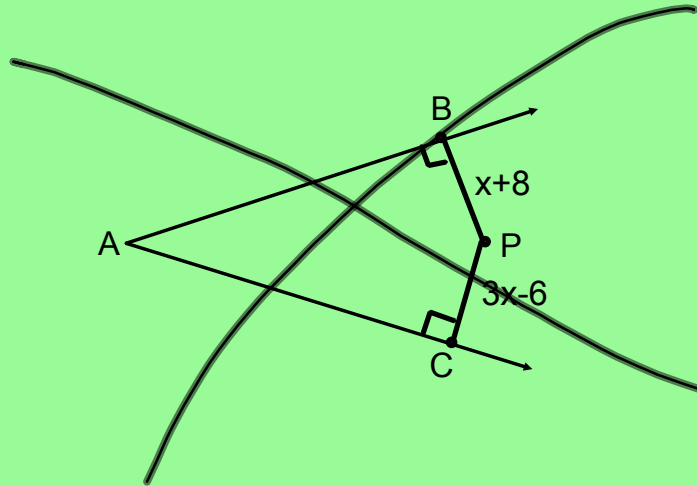
Can you conclude that \overrightarrow{BD} bisects $\angle ABC$? Explain.

No. Not enough info



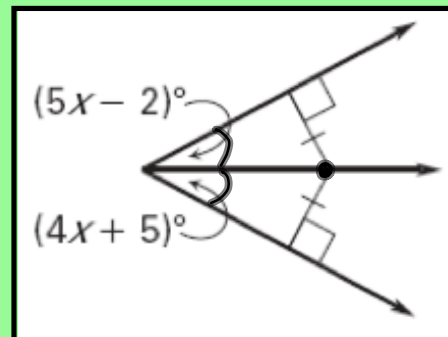
No. We don't know $\overline{DA} \perp \overline{BA}$ & $\overline{DC} \perp \overline{BC}$



Use Algebra to Solve a ProblemFind the value of x .

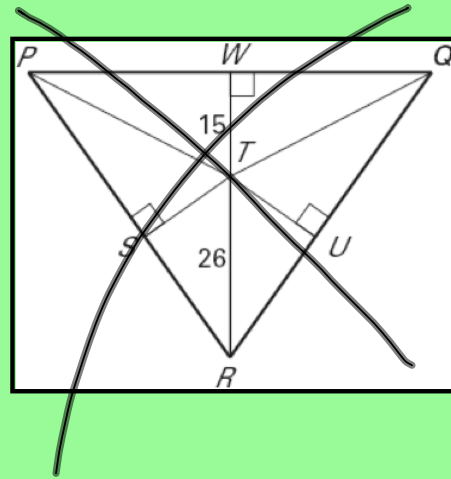
$$5x - 2 = 4x + 5$$

$$x = 7$$



Use the Concurrency of Angle Bisectors

Point T is the incenter of $\triangle PQR$. Find ST .



In the diagram, G is the incenter of $\triangle RST$. Find GW .

$$a^2 + b^2 = c^2$$

$$a^2 + 12^2 = 13^2$$

$$a^2 + 144 = 169$$

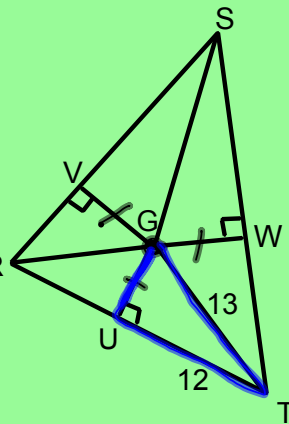
$$\begin{array}{r} -144 \\ -144 \end{array}$$

$$\sqrt{a^2} = \sqrt{25}$$

$$a = 5$$

$$GU = 5$$

$$GW = 5$$



Homework Assignment

Worksheet 5.3B

