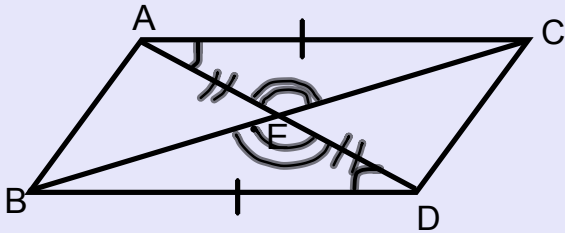


Bellwork

10/25/2011

Tell which triangles you can show are congruent in order to prove $\overline{AE} \cong \overline{DE}$. What postulate or theorem would you use?

1.



$\triangle AEC \cong \triangle DEB$
AAS Thm.

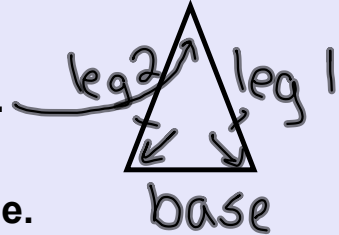
Geometry

4.7 Use Isosceles and Equilateral Triangles

Standard(s): 3,7

Vocabulary:

1. **Legs:** The two congruent sides of an isosceles triangle.
2. **Vertex Angle:** The angle formed by the legs.
3. **Base:** The third side of the isosceles triangle.
4. **Base Angles:** The two angles adjacent to the base.



THEOREMS

For Your Notebook

THEOREM 4.7 Base Angles Theorem

If two sides of a triangle are congruent, then the angles opposite them are congruent.

If $\overline{AB} \cong \overline{AC}$, then $\angle B \cong \angle C$.

Proof: p. 265



THEOREM 4.8 Converse of Base Angles Theorem

If two angles of a triangle are congruent, then the sides opposite them are congruent.

If $\angle B \cong \angle C$, then $\overline{AB} \cong \overline{AC}$.

Proof: Ex. 45, p. 269



COROLLARIES

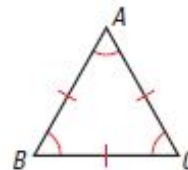
For Your Notebook

Corollary to the Base Angles Theorem

If a triangle is equilateral, then it is equiangular.

Corollary to the Converse of Base Angles Theorem

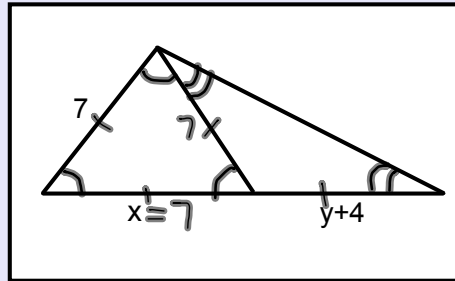
If a triangle is equiangular, then it is equilateral.



NOTE: If a \triangle is equiangular, then the measure of each $\angle = 60^\circ$

Use Isosceles and Equilateral Triangles

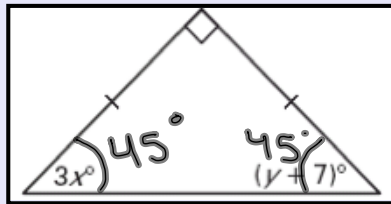
If possible, find the values of x and y in the diagram. Explain the reasoning.



$$x = 7$$

$$y + 4 = 7$$

$$y = 3$$



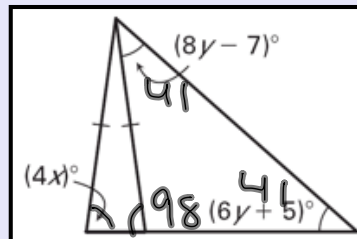
$$3x = 45$$

$$x = 15$$

$$3x = y + 7$$

$$y + 7 = 45$$

$$y = 38$$



$$8y - 7 = 6y + 5$$

$$2y = 12$$

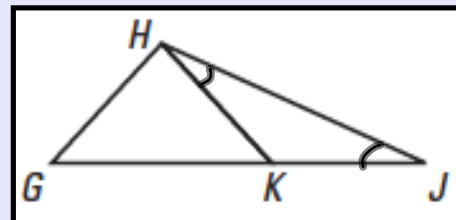
$$y = 6$$

$$4x = 82$$

$$x = 20.5$$

Apply the Base Angles Theorem

Copy and complete the statement.



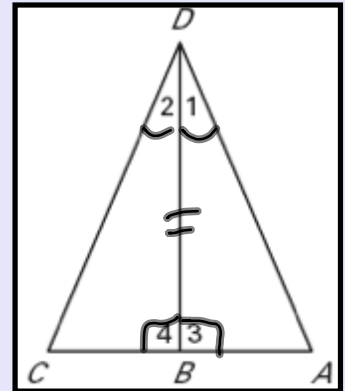
1. If $\overline{HG} \cong \overline{HK}$, then $\angle \underline{HGK} \cong \angle \underline{HKG}$.

2. If $\angle KHJ \cong \angle KJH$, then $\underline{\overline{HK}} \cong \underline{\overline{JK}}$.

Solve a Multi-Step Problem

Given: \overline{BD} bisects $\angle ADC$
 $\overline{DB} \perp \overline{AC}$

Prove: $\triangle ADC$ is isosceles



- | | |
|--|---|
| <p>1. \overline{BD} bisects $\angle ADC$
 $\overline{DB} \perp \overline{AC}$</p> | <p>1. Given</p> |
| <p>2. $\angle 1 \cong \angle 2$</p> | <p>2. Def. of an \angle bisector</p> |
| <p>3. $\overline{DB} \cong \overline{DB}$</p> | <p>3. Reflexive</p> |
| <p>4. $\angle 4$ is a right \angle
 $\angle 3$ is a right \angle</p> | <p>4. Def. of \perp lines</p> |
| <p>5. $\angle 4 \cong \angle 3$</p> | <p>5. Right \angle's \cong them</p> |
| <p>6. $\triangle BDC \cong \triangle BDA$</p> | <p>6. ASA Post.</p> |
| <p>7. $\overline{DC} \cong \overline{DA}$</p> | <p>7. CPCTC</p> |
| <p>8. $\triangle ADC$ is isosceles</p> | <p>8. Def. of an isosceles \triangle</p> |

Homework Assignment

Worksheet 4.7B

